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# Mathematical modeling and performance analysis of the parabolic solar collector

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**Abstract:** In nowadays there are several types of solar collectors have already been developed. The parabolic cylindrical solar collector is used to increase the temperature of the fluid (air / water). In the present of our work, a parabolic cylindrical solar collector has been fabricated using the standard methodology proposed for the construction of conventional solar heaters. The variation in solar radiation, the air outlet temperature and the variation in the temperature of the absorbent plate throughout the day were recorded. The efficiency, effective optical efficiency and effective heat loss coefficient of the single cover flat plate solar collector were calculated. The effect of wind speed on the performance of the sensor was also studied.

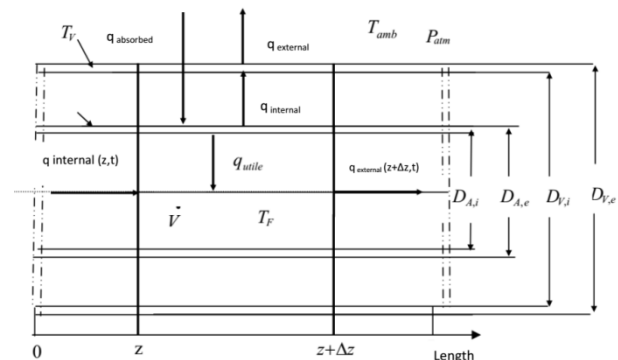
**Key words:** Absorber, Parabolic trough, solar receiver

## 1. Introduction

In the work present, a cylindrical parabolic solar collector is fabricated using the methodology used in the construction of conventional solar fan heaters [1-2-3]. The variation in solar radiation, the air outlet temperature and the variation in the absorbent temperature throughout the day were checked in. The efficiency, effective optical efficiency and effective heat loss coefficient of the parabolic cylinder solar collector are calculated and the effect of wind speed on collector performance is also studied [4-5-6].

## 2. Modeling of the cylindro-parabolic sensor:

The most important element in concentrator systems is the absorber tube in which the coolant circulates inside. The absorber tube is often made of copper covered with an appropriate selective layer and surrounded by a glass tube, as shown in Figure 1 by the differential equations of the three temperatures:  $T_F$  (Fluid),  $T_A$  (absorber) and  $T_V$  (glass), these equations vary during the time  $t$  (the time illumination) for a length  $z$  of the absorber.



**Figure.1:** Thermal balance of a surface element of the cylindro manifold parabolic

### 2.1. Choice of a mathematical method of resolution:

There are several ways to discretely We have chosen the finite difference method. The quantities  $y_q$  in our case are the temperature of the heat transfer fluid, and the temperature of the absorber as well as the temperature of the glazing, they are all a function of time and position. In general, we express the first partial derivative with respect to time as following:

$$\frac{dy_q}{dt} = \frac{y_q(z,t) - y_q(z,t-\Delta t)}{\Delta t} \quad (1)$$

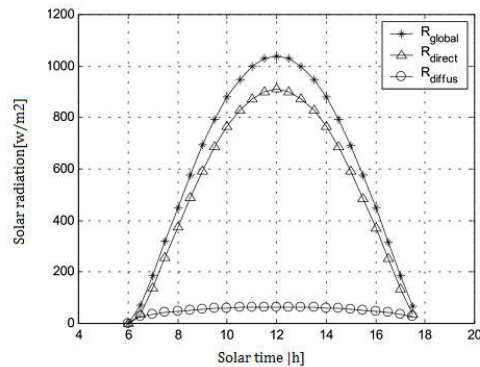
The partial derivative with respect to the abscissa  $z$ .

### 3. Results and discussions

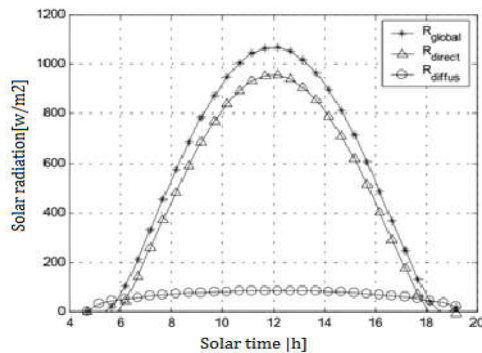
The numerical calculation method used constitutes a means for the determination of the outlet temperature of the fluid (water) in the absorber of a collector with a concentration effect of the parabolic cylindrical type.

#### 3.1 Solar radiation:

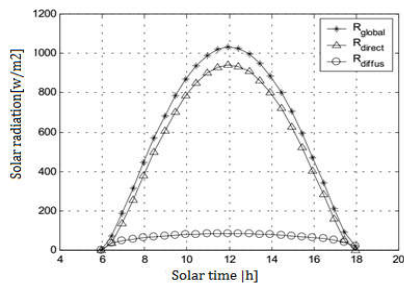
We represent the curves of figures (2, 3, 4, and 5) which reflect the variation of the global radiation, direct and diffuse during four typical days of the year 2020, by adopting the correlation between the localization in Tunisia.



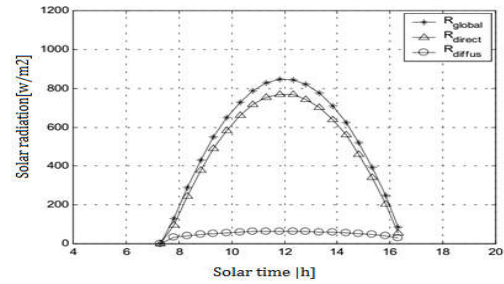
**Figure.2:** Evolution of global, diffuse and direct radiation as a function of time for the day March 21



**Figure .3 :** Evolution of global, diffuse and direct radiation as a function of time for June 21.



**Figure.4 :** Evolution of global, diffuse and direct radiation as a function of time for the day September 21.



**Figure .5:** Evolution of global, diffuse and direct radiation as a function of time for December 21.

We note that for the day of June 21, the global radiation is maximum at true solar noon which can reach  $1100 \text{ W / m}^2$ . For the modeling of the outlet temperature, only direct radiation will be taken into account.

### Conclusion

In the present work, a parabolic cylindrical solar collector has been studied by a mathematical study of the optical efficiency and the effective heat loss coefficient of the parabolic cylinder solar collector are calculated and the effect of wind speed on sensor performance is also investigated.

### References

- [1] Ong K S 1995 Thermal performance of solar air heaters: Mathematical model and solution procedure. *Sol. Energy* 55 93–109.
- [2] Yousef B A A, Adam N M 2012 Performance and cost analysis of double duct solar air heaters. *Int. J. Sci. Technol. Res.* 1 108–116.
- [3] Jannot Y, Coulibaly Y 1997 Radiative heat transfer in a solar air heater covered with a plastic film. *Sol. Energy* 60 35–40.
- [4] Choudhury C, Chauhan P M, Garg H P 1995 Design curves for conventional solar air heaters. *Renew. Energy* 6 739–749.
- [5] Saedodin S, Zamzamian S A H, Nimvari M E, Wongwises S, Jouybari H J 2017 Performance evaluation of a flatplate solar collector filled with porous metal foam: Experimental and numerical analysis. *Energy Convers. Manag.* 153 278–287.
- [6] Nikolić N, Lukić N 2015 Theoretical and experimental investigation of the thermal performance of a double exposure flat-plate solar collector. *Sol. Energy* 119 100–113.